

Chapter 6

#7

Origin	Destination				Capacities
	Boston	Dallas	Los Angeles	St. Paul	
Denver	7	11	8	13	} 350
Atlanta	20	17	12	10	
Chicago	8	18	13	16	
<u>Demands</u>	50	70	60	80	

260

Let X_{ij} = # units shipped from origin i to destination j

Min $7X_{11} + 11X_{12} + 8X_{13} + 13X_{14} + 20X_{21} + 17X_{22} + 12X_{23} + 10X_{24}$
 $+ 8X_{31} + 18X_{32} + 13X_{33} + 16X_{34}$

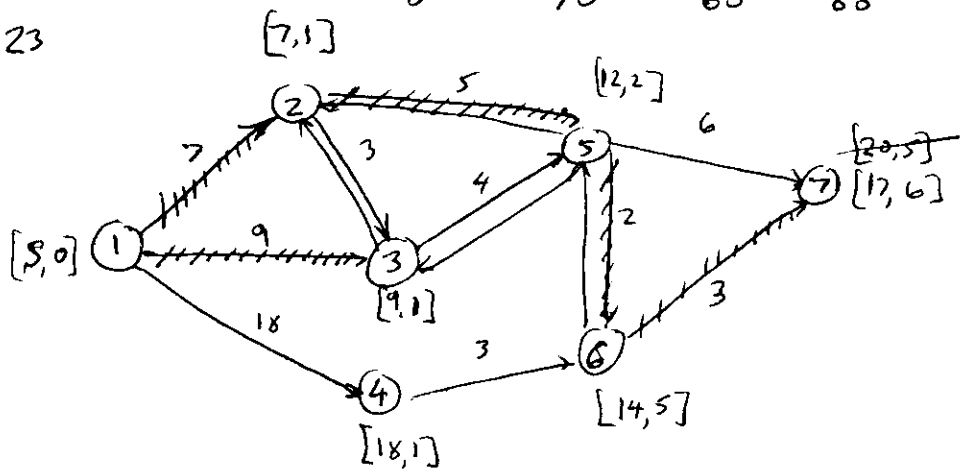
s.t. $X_{11} + X_{12} + X_{13} + X_{14} \leq 100$
 $X_{21} + X_{22} + X_{23} + X_{24} \leq 100$
 $X_{31} + X_{32} + X_{33} + X_{34} \leq 150$
 $X_{11} + X_{21} + X_{31} = 50$
 $X_{12} + X_{22} + X_{32} = 70$
 $X_{13} + X_{23} + X_{33} = 60$
 $X_{14} + X_{24} + X_{34} = 80$

Solution

	Boston	Dallas	LA	St. Paul	
Denver	0	70	30	0	100
Atlanta	0	0	20	80	100
Chicago	50	0	10	0	60
	50	70	60	80	

Total Cost
82,580

#23



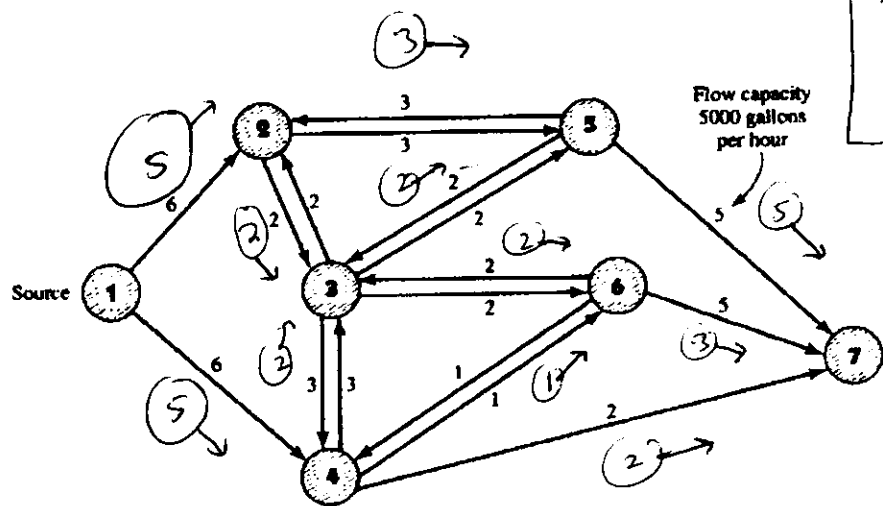
Solution
 $X_{12} = X_{25} = X_{56} = X_{67} = 1$
 all others are 0

Done as Lin. Prog. Min $7X_{12} + 9X_{13} + 18X_{14} + 3X_{23} + 5X_{25} + 3X_{32} + 4X_{35} + 3X_{46}$
 $+ 5X_{52} + 4X_{53} + 2X_{56} + 6X_{57} + 2X_{65} + 3X_{67}$

s.t. $X_{12} + X_{13} + X_{14} = 1$ and $-X_{12} + X_{23} + X_{25} = 0$ $-X_{56} - X_{46} + X_{65} + X_{67} = 0$
 $X_{57} + X_{67} = 1$ $-X_{13} - X_{23} + X_{32} + X_{35} = 0$
 $-X_{14} + X_{46} = 0$ $-X_{25} - X_{35} + X_{52} + X_{53} + X_{56} + X_{57} = 0$

#32 (also as a Power Point - old chap 9 #18)

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MAX 1x71

s.t.

- Node (1) $1x12 - 1x14 - 1x71 = 0$
- Node (2) $-1x12 - 1x23 - 1x32 + 1x25 - 1x52 = 0$
- Node (3) $-1x23 + 1x32 + 1x34 - 1x43 - 1x35 - 1x53 - 1x36 - 1x63 = 0$
- Node (4) $-1x14 - 1x34 + 1x43 - 1x46 - 1x64 + 1x47 = 0$
- Node (5) $-1x25 - 1x52 - 1x35 - 1x53 - 1x57 = 0$
- Node (6) $-1x36 - 1x63 - 1x46 - 1x64 + 1x67 = 0$
- Node (7) $-1x47 - 1x57 - 1x67 - 1x71 = 0$
- (8) $1x12 \leq 6$
- (9) $1x14 \leq 6$
- (10) $1x23 \leq 2$
- (11) $1x32 \leq 2$
- (12) $1x25 \leq 3$
- (13) $1x52 \leq 3$
- (14) $1x34 \leq 3$
- (15) $1x43 \leq 3$
- (16) $1x35 \leq 2$
- (17) $1x53 \leq 2$
- (18) $1x36 \leq 2$
- (19) $1x63 \leq 2$
- (20) $1x46 \leq 1$
- (21) $1x64 \leq 1$
- (22) $1x47 \leq 2$
- (23) $1x57 \leq 5$
- (24) $1x67 \leq 5$

OPTIMAL SOLUTION

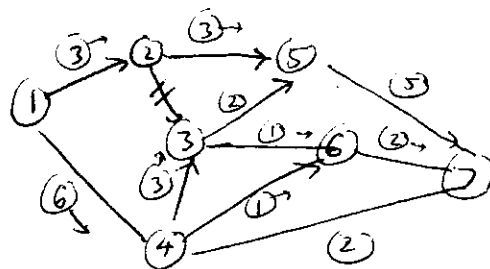
Objective Function Value = 10.000

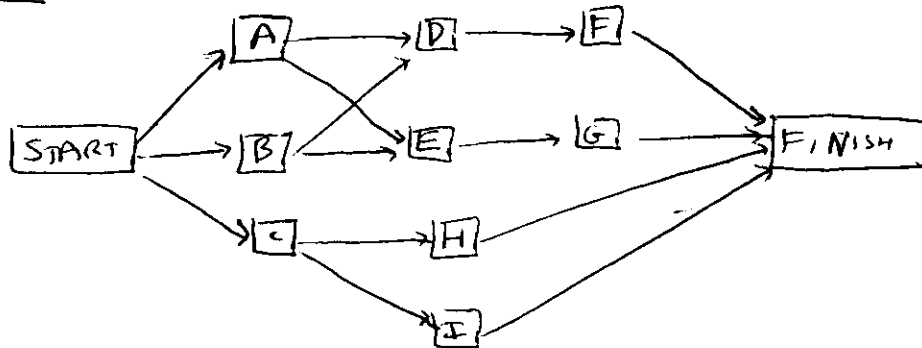
Variable	Value
x12	5.000
x14	5.000
x23	2.000
x32	0.000
x25	3.000
x52	0.000
x34	0.000
x43	2.000
x35	2.000
x53	0.000
x36	2.000
x63	0.000
x46	1.000
x64	0.000
x47	2.000
x57	5.000
x67	3.000
x71	10.000

(a) $100,000 / 10,000 = 10$ hrs

(b) See Power Point $100,000 / 9,000 = 11.1$ hrs.

new solution has





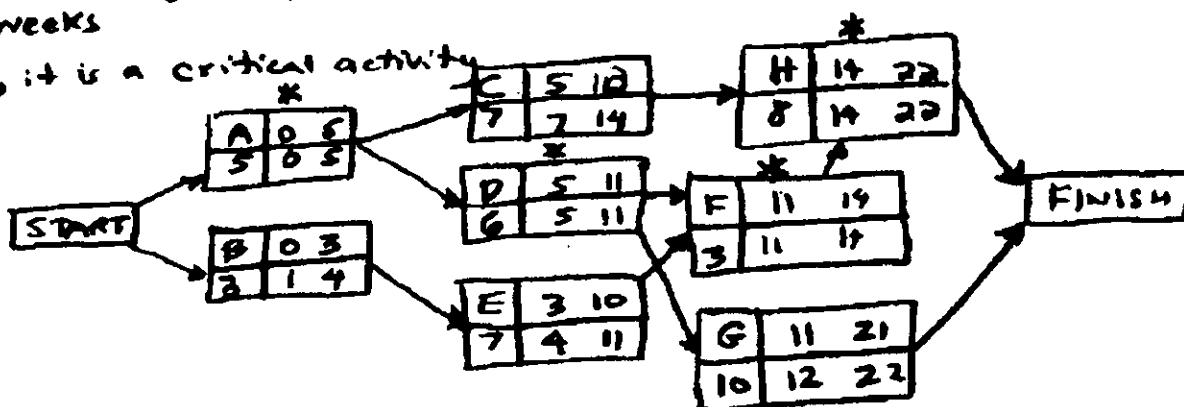
14) possible paths

A-C-H	5+7+8	= 20
A-D-F-H	5+6+3+8	= 22 *
A-D-G	5+6+10	= 21
B-E-F-H	3+7+3+8	= 21
B-E-G	3+7+10	= 20

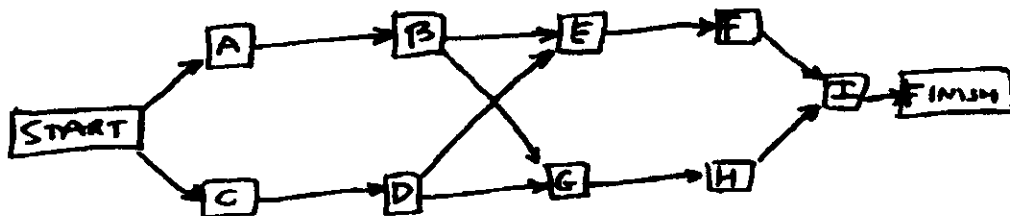
(b) 22 weeks

(c) NO, it is a critical activity

(d)



15) (a)



(b)

Activity	$t = \frac{a+4m+b}{6}$	$V = \frac{(b-a)^2}{36}$
A	2	0,03
B	$\frac{2+4(2,3)+6}{6} = 3$	0,44
C	2	0,11
D	2	0,03
E	1	0,03
F	2	0,11
G	4	0,44
H	4	0,11
I	2	0,03

ACTIVITY	ES	EF	LS	LF	Slack
A	0	2	0	2	0
B	2	5	2	5	0
C	0	2	0	2	0
D	2	4	3	5	1
E	5	8	10	11	5
F	6	8	11	13	5
G	5	9	5	9	0
H	9	13	9	13	0
I	13	15	13	14	0

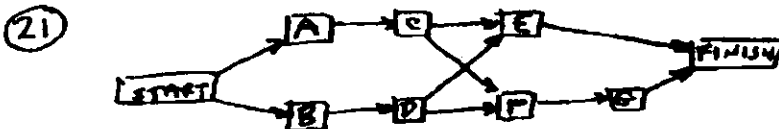
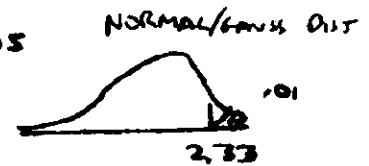
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(C) E(T) A-B-G-H-I (15)

(B) $\sigma^2 = 0.03 + 0.44 + 0.44 + 0.11 + 0.03 = 1.05$

$Z = \frac{T - 15}{\sqrt{1.05}} = 2.33$

$T = 15 + 2.33\sqrt{1.05} = 17.4$ weeks



ACTIVITY	A	B	C	D	E	F	G
TIME	3	2	5	5	6	2	2

(a)

ACTIVITY	ES	EF	LS	LF	Slack
A	0	3	0	3	0
B	3	5	3	5	0
C	0	5	0	5	0
D	3	8	3	8	0
E	5	11	5	11	0
F	8	10	8	10	0
G	10	12	10	12	0

A-C-E

$3 + 5 + 6 = 14$ days

(b) Cost total = \$ 8,400

(b)

Act.	Cost	Cost/Day
C	400	400
E	500	500
	900	

(22)

(a)

ACTIVITY	MAX CAPACITY DAYS	COST/DAY
C	2	600
D	2	700
E	2	400
F	2	400
G	2	500
H	2	400
I	2	500

(c) Total Cost = $8400 + 900 = 9,300$

	pl-#1	pl-#2	pl-#3
ACE	14	13	12
ACFG	12	11	11
BDE	13	13	12
BDFG	11	11	11

CHAP 11

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 A, S, & W

① (a) $\lambda = 0.4 (5) = 2$ per five minute period

(b)	$P(x) = \frac{\lambda^x e^{-\lambda}}{x!}$	x	$P(x)$	} .8571
		0	0.1353	
		1	0.2707	
		2	0.2707	
		3	0.1804	

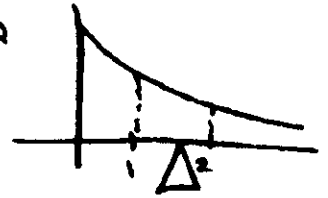
(c) $P(\text{Delay Problems}) = P(X > 3) = 1 - P(X \leq 3) = 1 - .8571 = \boxed{0.1429}$

② (a) $\mu = 0.6$ customers/min

$P(\text{service time} \leq 1) = 1 - e^{-0.6(1)} = \underline{0.4512}$

(b) $P(\text{s.t.} \leq 2) = 1 - e^{-0.6(2)} = \underline{0.6988}$

(c) $P(\text{s.t.} > 2) = 1 - .6988 = \underline{0.3012}$



③ (a) $P_0 = 1 - \frac{\lambda}{\mu} = 1 - \frac{0.4}{0.6} = \underline{0.3333}$

(b) $L_q = \frac{\lambda^2}{\mu(\mu-\lambda)} = \frac{(0.4)^2}{0.6(0.6-0.4)} = \underline{1.3333}$

(c) $L = L_q + \frac{\lambda}{\mu} = 1.3333 + \frac{0.4}{0.6} = \underline{2}$

(d) $W_q = \frac{L_q}{\lambda} = \frac{1.3333}{0.4} = \underline{3.333}$ min

(e) $W = W_q + \frac{1}{\mu} = 3.333 + \frac{1}{0.6} = \underline{5}$ min

(f) $P_w = \frac{\lambda}{\mu} = \frac{0.4}{0.6} = \underline{0.6667}$

②②

$\lambda = 24$ cust/hr

(A) $\mu = 30$ cust/hr (2 mins)

(B) $\mu = 48$ cust/hr (1.25 mins)

(C) $K=2$ $\mu = 30$ cust/hr (2 mins) for each channel

(a) $P_0 = \frac{A}{0.2} \quad \frac{B}{0.5} \quad \frac{C}{0.4286}$

(A) $P_0 = 1 - \frac{\lambda}{\mu} = 1 - \frac{24}{30} = 0.2$

(B) $P_0 = 1 - \frac{\lambda}{\mu} = 1 - \frac{24}{48} = 0.5$

(c) from table $\lambda/\mu = 0.8$ $K=2$

(b) $L_q = \frac{3.2}{0.5} \quad \frac{0.5}{0.5} \quad \frac{0.1524}{0.5}$

(A) $L_q = \frac{\lambda^2}{\mu(\mu-\lambda)} = \frac{24^2}{30(30-24)} = \frac{576}{180} = 3.2$

(B) $L_q = \frac{24^2}{48(48-24)} = \frac{576}{1152} = 0.5$

for (C) $L_q = \frac{(\frac{\lambda}{K})^2 \lambda \mu}{K!(2\mu-\lambda)^2} P_0 = \frac{(\frac{24}{30})^2 24(30)}{1(60-24)^2} P_0 = \frac{16}{45} (0.4286) = 0.1524$

(c) $L = \frac{A}{4.0} \quad \frac{B}{1.0} \quad \frac{C}{0.9534}$ $L = L_q + \frac{\lambda}{\mu}$ for all cases

(d) $W_q = 0.1333 \text{ hr (8 mins)} \quad 0.0208 \text{ hr (1.25 mins)} \quad 0.0063 \text{ hr (0.38 min)}$ $W_q = \frac{L_q}{\lambda}$ for all

(e) $W = 0.1667 \text{ (10 mins)} \quad 0.0417 \text{ (2.5 mins)} \quad 0.0397 \text{ (2.38 mins)}$ $W = W_q + \frac{1}{\mu}$

(f) $P_w = \underline{0.8} \quad \underline{0.5} \quad 0.2286$
 $\uparrow \uparrow$
best server

(A) $P_w = \lambda/\mu = 24/30 = 0.8$
 (B) $P_w = \lambda/\mu = 24/48 = 0.5$
 (C) $P_w = \frac{1}{2!} \left(\frac{24}{30}\right)^2 \left(\frac{2(30)}{2(30)-24}\right) P_0 = 0.2286$
 \uparrow
 (0.2286)

(24) Customer time \$ 25/hr for waiting time
 Employee \$ 6.50/hr
 Channel costs \$ 20/hr each

(A) $3.2 \xrightarrow{L_q} (25) = \80.00 (all customers) n 1 hr
 + (1) (6.50) = 6.50
 + (1) (20) = 20.00
 $\underline{\hspace{1cm}}$
 \$ 106.50/hr

(B) $0.5 (25) = 12.50$
 (2) (6.50) = 13.00
 (1) (20) = 20.00
 $\underline{\hspace{1cm}}$
 \$ 45.50/hr \leftarrow best bottom line

(C) $0.1524 (25) = 3.81$
 (2) (6.50) = 13.00
 (2) (20) = 40.00
 $\underline{\hspace{1cm}}$
 \$ 56.81/hr

Chapter 15

MBA 515 (21)
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 HW Answers
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Week	Sales	4 wk mov avg	error ²	5 wk mov avg	error ²
1	17				
#2 2	21				
3	19				
4	23				
(A) 5	18	20.00	4.00		
6	16	20.25	18.06	19.6	12.96
7	20	19.00	1.00	19.4	0.36
8	18	19.25	1.56	19.2	1.44
9	22	18.00	16.00	19.0	9.00
10	20	19.00	1.00	18.8	1.44
11	15	20.00	25.00	19.2	17.64
12	22	18.75	10.56	19.0	9.00
			<u>77.19</u>		<u>51.84</u>

(B) $MSE_4 = \frac{77.19}{8} = 9.65$

$MSE_5 = \frac{51.84}{7} = 7.41$

(C) 5-week Moving Average is Better

Week	Sales	Weighted Mov Average	error ²
1	17		
2	21		
3	19		
4	23	19.33	13.44
5	18	21.33	11.11
6	16	19.83	14.69
7	20	17.83	4.69
8	18	18.33	0.11
9	22	18.33	13.44
10	20	20.33	0.11
11	15	20.33	28.44
12	22	17.83	17.36
			<u>103.42</u>

(B) $MSE_3 = \frac{103.42}{9} = 11.49$

Unweighted MSE = 10.22 ← better

(C) There is always some weighted average that is at least as good (note $w_1 = w_2 = w_3 = \frac{1}{3}$ is a special case)

USING SOLVER in EXCEL
 $w_1 = 0.1257$ $w_2 = 0.3603$ $w_3 = 0.5140$ (most recent)
 produces MSE = 9.696

Week	Sales	Exp Moving Avg $\alpha = 0.1$	error ²	Exp Moving Avg $\alpha = 0.2$	error ²	$\alpha = 0.1744$	error ²	optimal α by SOLVER
1	17							
2	21	17.00	16.00	17.00	16.00	17.00	16.00	
3	19	17.40	2.56	17.80	1.44	17.70	1.70	
4	23	17.56	29.59	18.04	24.60	17.92	25.76	
5	18	18.10	0.01	19.03	1.07	18.81	0.66	
6	16	18.09	4.38	18.83	7.98	18.67	7.12	
7	20	17.88	4.48	18.26	3.03	18.20	3.23	
8	18	18.10	0.01	18.61	0.37	18.52	0.27	
9	22	18.09	15.32	18.49	12.34	18.43	12.77	
10	20	18.48	2.32	19.19	0.66	19.05	0.90	
11	15	18.63	13.18	19.35	18.94	19.22	17.77	
12	22	18.27	13.94	18.48	12.38	18.48	12.39	
			<u>101.78</u>		<u>98.80</u>		<u>98.56</u>	
		Sum						
		MSE	9.25		8.98		8.96	← least

$\alpha = 0.2$ had a lower MSE than $\alpha = 0.1$ but the best is $\alpha = 0.1744$

#14

t	Y
1	20.5
2	20.2
3	19.5
4	19.0
5	19.1
6	18.8

n = 6
 $\sum Y = 117.1$
 $\sum t = 21$
 $\sum t^2 = 91$
 $\sum tY = 403.7$

$$b_1 = \frac{n \sum tY - (\sum t)(\sum Y)}{n \sum t^2 - (\sum t)^2} = \frac{6(403.7) - 21(117.1)}{6(91) - (21)^2} = -0.3514$$

$$b_0 = \bar{Y} - b_1 \bar{t} = 19.5167 - (-0.3514)(3.5) = 20.7466$$

$$\hat{Y} = 20.7466 - 0.3514t$$

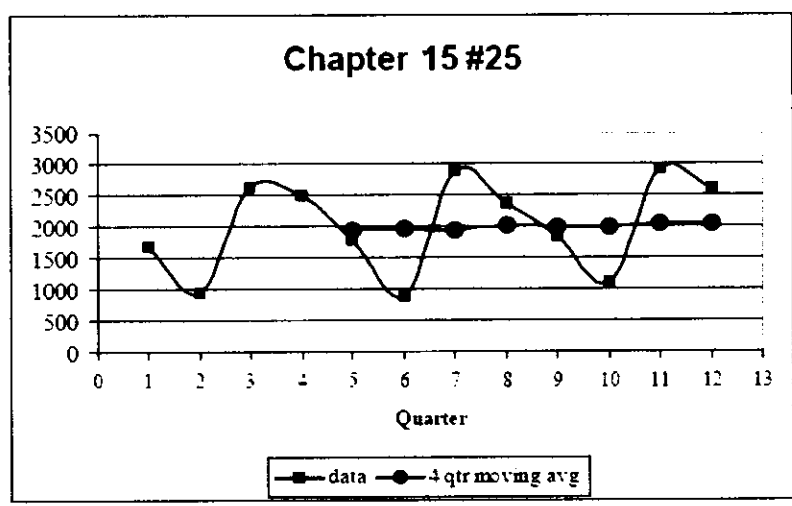
Conclusion enrollment is decreasing by 351/yr

#25

Prof. Richard B. Goldstein							
	A	B	C	D	E	F	G
1					4-Qtr Moving	Ctr Mov	Data: CMA
2	Period	Year	Qtr	Data	Average	Average	Ratio
3	1	1	1	1690			
4	2	1	2	940			
5	3	1	3	2625		1952.500	1.34443
6	4	1	4	2500		1961.250	1.27470
7	5	2	1	1800	1938.75	1990.625	0.90420
8	6	2	2	900	1966.25	2007.500	0.44832
9	7	2	3	2900	1956.25	1996.250	1.45272
10	8	2	4	2360	2025.00	2027.500	1.16400
11	9	3	1	1850	1990.00	2056.250	0.89970
12	10	3	2	1100	2002.50	2091.875	0.52584
13	11	3	3	2930	2052.50		
14	12	3	4	2615	2060.00		
15	13						
16	14						
17						Seasonal Index	
18						Unadjusted	Adjusted
19						0.901967	0.900398
20						0.487081	0.486234
21						1.398577	1.396144
22						1.219346	1.217225
23						4.006972	4.000000

E7: =AVERAGE(D3:D6)
 F5: =(D3+2*SUM(D4:D6)+D7)/8
 G5: =D5:F5

F19: =(G7+G11)/2
 G19: =F21*4-FS25
 F23: =SUM(F19:F22)



Chapter 12

MBA 515 (23)
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#6	Payment	Prob.	Cumul. prob.	R interval
	\$ 0	0.83	0.83	[0, 0.83]
	500	0.06	0.89	(0.83, 0.89]
	1,000	0.05	0.94	(0.89, 0.94]
	2,000	0.02	0.96	(0.94, 0.96]
	5,000	0.02	0.98	(0.96, 0.98]
	8,000	0.01	0.99	(0.98, 0.99]
	10,000	0.01	1.00	(0.99, 1.00]

4 claims totaling
 \$ 22,000

0.9850 \Rightarrow \$ 8,000	0.4971 \Rightarrow 0
0.2122 \Rightarrow 0	0.9569 \Rightarrow \$ 2,000
0.5590 \Rightarrow 0	0.1091 \Rightarrow 0
0.0004 \Rightarrow 0	0.9907 \Rightarrow 10,000
0.5177 \Rightarrow 0	0.1900 \Rightarrow 0
0.0064 \Rightarrow 0	0.9903 \Rightarrow 2,000
0.2044 \Rightarrow 0	0.7545 \Rightarrow 0
0.2390 \Rightarrow 0	0.8083 \Rightarrow 0
0.7305 \Rightarrow 0	0.9204 \Rightarrow 0
0.6351 \Rightarrow 0	0.5274 \Rightarrow 0

#9

- (a) base or most likely case:
 $6 + 5 + 14 + 8 = 33$ weeks
 Worst case:
 $8 + 7 + 18 + 10 = 43$ weeks
 best case:
 $5 + 3 + 10 + 8 = 26$ weeks

- (b) activity random no.
- | | |
|---|---|
| A | 0.1778 in (0, 0.25] \Rightarrow 5 wks |
| B | 0.9617 in (0.75, 1.00) \Rightarrow 7 |
| C | 0.6849 in (0.35, 0.75) \Rightarrow 14 |
| D | 0.4503 in (0.00, 0.60) \Rightarrow 8 |
- 34 weeks

- (c) SIMULATION WILL PROVIDE A DISTRIBUTION OF PROJECT COMPLETION TIME VALUES. IN (b) THERE IS ONE SUCH CASE WITH THE FOUR ACTIVITIES - AT LEAST 100 SUCH CASES SHOULD BE DONE, THEN, THE PERCENTAGE OF SIMULATION CASES WITH COMPLETION TIMES OF 35 WEEKS OR LESS CAN BE USED TO ESTIMATE THE ACTUAL PROBABILITY.

#18

A: U [600, 800]

B: Normal $\mu = 700$
 $\sigma = 50$ MBA 515 (24)
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	A	B	C	D	E	F	G	H
1	Contractor Bidding							
2								
3	Contractor A (Uniform Distribution)				Contractor B (Normal Distribution)			
4	Smallest Value		600			Mean		700
5	Largest Value		800			Standard Deviation		50
6								
7								
8	Simulation				Results			
9		Contractor	Contractor	Lowest		Contractor's	Number	Probability
10	Trial	A's Bid	B's Bid	Bid		Bid	of Wins	of Winning
11	1	744	717	717		\$650	636	0.636
12	2	660	748	660		\$625	820	0.82
13	3	693	708	693		\$615	893	0.893
14	4	751	713	713				
15	5	623	645	623				
16	6	665	706	665				

Cells:

$$B_{11} = C_{84} + \text{RAND}() * (C_{85} - C_{84})$$

$$C_{11} = \text{NORMINV}(\text{RAND}(), H_{84}, H_{85})$$

$$D_{11} = \text{MIN}(B_{11}, C_{11})$$

$$G_{11} = \text{COUNTIF}(\$D\$11:\$D\$1010, ">650")$$

$$H_{11} = G_{11} / 1000$$

} copy to row 1010

- (a) \$650,000 is the winning bid 636/1000 (text ≈ 0.60 to 0.65)
 (b) 625,000 " " " " 820/1000 (text ≈ 0.82)
 (c) 615,000 " " " " 893/1000 (text ≈ 0.88)

$$P(X_1 > 650 \wedge X_2 > 650) = \left(\frac{150}{200}\right) P\left(Z > \frac{650 - 700}{50}\right) = 0.75(0.8413) = \underline{\underline{0.631}}$$

$$P(X_1 > 625 \wedge X_2 > 625) = \left(\frac{175}{200}\right) P\left(Z > \frac{625 - 700}{50}\right) = 0.875(0.933) = \underline{\underline{0.816}}$$

$$P(X_1 > 615 \wedge X_2 > 615) = \left(\frac{185}{200}\right) P\left(Z > \frac{615 - 700}{50}\right) = 0.925(0.9554) = \underline{\underline{0.884}}$$