

Business 515 - Computer Take-Home Problems - Prof. Richard B. Goldstein

#1 LINEAR PROGRAMMING (10%)

Sunshine Juices sells three juice mixtures: Tropical Blend, Hawaiian Blend, and Florida Special. Tropical Blend contains a mixture of orange, grapefruit, pineapple, and guava juices. Hawaiian Blend contains a mixture of grapefruit, pineapple, and guava juices. Florida Special is a mixture of only orange and grapefruit juices.

The cost of each juice is as follows:

orange	\$4.40/gallon
grapefruit	4.00/gallon
pineapple	4.90/gallon
guava	6.40/gallon

and the blends sell for:

Tropical Blend	\$7.20/gallon
Hawaiian Blend	6.70/gallon
Florida Special	5.40/gallon

Available at the moment are [eq #1] 1,500 gallons of orange juice, [eq #2] 900 gallons of grapefruit juice, [eq #3] 600 gallons of pineapple juice, and [eq #4] 600 gallons of guava juice. There is a demand for at least [eq #5] 900 gallons of Tropical Blend, [eq #6] 600 gallons of Hawaiian Blend, and [eq #7] 1,200 gallons of Florida Special.

The mixing conditions for Tropical Blend [eq #8] require at least 30% orange juice, [eq #9] at least 20% grapefruit juice, and [eq #10] at least 20% guava juice. Similarly, Hawaiian Blend must contain [eq #11] at least 25% grapefruit juice, [eq #12] at least 40% pineapple juice, and [eq #13] at most 50% pineapple juice. Finally, Florida Special must contain at [eq #14] least 40% orange juice and [eq #15] at most 70% orange juice.

HINT Let X_1 = Gallons of orange juice in Tropical Blend
 X_2 = Gallons of grapefruit juice in Tropical Blend
: = :
 X_9 = Gallons of grapefruit juice in Florida Special

QUESTIONS:

- (1) What is the maximum profit?
- (2) How many gallons of each juice are used?
- (3) How many gallons of each Blend are sold?
- (4) What is the percentage of each juice used in each of the Blends?
- (5) How much more profit can be made with one additional gallon of orange juice?
Repeat for guava juice.

#2 DECISION ANALYSIS (10%)

The Palm Garden Greenhouse specializes in raising carnations that are sold to florists. Carnations are sold for \$18 per dozen; the cost of growing the carnations and distributing them to the florists is \$11 per dozen. Any carnations left at the end of the day are sold to local restaurants and hotels for \$6 per dozen. The estimated cost of customer ill-will when demand is not met is \$8 per dozen. The expected daily demand (in dozens) for the carnations is shown below.

<u>Daily Demand</u>	<u>Probability</u>
20	0.15
25	0.25
30	0.40
35	0.15
40	<u>0.05</u>
	1.00

- A. Develop the 5 X 5 payoff table for this decision problem.
- B. Compute the **expected value** of each alternative that could be stocked and select the best alternative. Compute the **Expected Value** with and of Perfect Information.
- C. Construct the **opportunity loss table** and determine the **minimax regret**.
- D. Find the best strategy **without** the probability information using
 - (I) OPTIMIST/maximax
 - (II) PESSIMIST/maximin
 - (III) HURWICZ/ $\alpha=0.4$ (not in package – use results from I and II)
 - (IV) LAPLACE/equally likely (change $p = 0.2$ for each)

#3 GAME THEORY (5%)

Consider the following zero-sum game payoff table for two players:

<u>Player I Strategies</u>	<u>Player II Strategies</u>				
	<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>	<u>E</u>
#1	5	3	-6	-2	9
#2	4	9	3	-7	-1
#3	1	1	4	3	0
#4	-5	6	7	9	-2

A pure strategy is not possible for this game. Determine the mixed strategy for each player using linear programming or http://people.hofstra.edu/faculty/Stefan_Waner/gametheory/games.html. Find the value of the game and the probabilities associated with each strategy.