

# LINEAR PROGRAMMING & NETWORKS – Prof. Richard B. Goldstein

## TRANSPORTATION

$\text{Min} \sum_{i=1}^m \sum_{j=1}^n c_{ij} x_{ij}$	$c_{ij}$ = cost of sending 1 item from $i$ to $j$ $x_{ij}$ = 0 or 1 where 1 indicates item is transported from $i$ to $j$
s.t. $\sum_{j=1}^n x_{ij} \leq q_i$ for all $i$	capacity limits at $i^{\text{th}}$ location
$\sum_{i=1}^m x_{ij} = r_j$ for all $j$	demand at $j^{\text{th}}$ locations

## ASSIGNMENT

$\text{Min} \sum_{i=1}^m \sum_{j=1}^n c_{ij} x_{ij}$	$c_{ij}$ = cost of assigning $i^{\text{th}}$ person the $j^{\text{th}}$ position $x_{ij}$ = 0 or 1 where 1 means $i^{\text{th}}$ person does $j^{\text{th}}$ position
s.t. $\sum_{j=1}^n x_{ij} \leq 1$ for all $i$	every job must be done
$\sum_{i=1}^m x_{ij} = 1$ for all $j$	everyone gets 1 job to do

## SHORTEST-ROUTE

$\text{Min} \sum_i \sum_j c_{ij} x_{ij}$	$c_{ij}$ = time/distance from node $i$ to node $j$	$x_{ij}$ = 0 or 1
s.t. $\sum_j x_{1j} = 1$	origin node – every optimal path must start here at node 1	
$\sum_i x_{ik} - \sum_j x_{kj} = 0$	amount in – amount out = 0 for all intermediate nodes $k$	
$\sum_j x_{jm} = 1$	final node – every optimal path must end here at node $m$	

## MAXIMAL FLOW

Max $x_{m1}$	final node $m$ back to node 1 where $x_{ij}$ = amount flowing from node $i$ to $j$	
s.t. $x_{ij} \leq q_{ij}$	less than maximum capacity from node $i$ to $j$ for all branches	
$\sum_i x_{ik} - \sum_j x_{kj} = 0$	flow in – flow out = 0 for all nodes $k$	